

E1-25 On the self-homotopy equivalences of $BO(n)$

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Let G be a compact Lie Group and BG be the classifying space of G . The study of self homotopy equivalences of BG has been an area that generated a large amount of interest during the last few years. Though extensive work has been done on connected Lie Groups, the case of non-connected groups remains largely untouched.

In this Paper, I will give a complete description of the self-homotopy equivalences of $(BO(2n)_2)$ ($BO(n)$ completed at the prime 2). When n is odd, $O(2n+1) \cong SO(2n+1) \times \mathbb{Z}/2\mathbb{Z}$ and the case reduces to one dealing with a connected group. Our focus therefore, will be on $O(2n)$. Our method of attack is based on the fact that every compact Lie Group G contains a maximal Torus T .

Let $W = NT/T$ W is called the Weyl group of G .

Let $N_2 \circ^{(2n)} T$ denote an extension of T by a 2-Sylow sub group of W . The fact is: even though a self homotopy equivalence of BG_2^\wedge need not appear as a group Homomorphism of G , it does appear as an admissible map $\phi: T_\gamma \rightarrow T_\gamma$ (where T_γ is the subgroup of T containing all elements of order a power of 2) and as a special type of representation $\rho: N_2 \circ^{(2n)} T \rightarrow G$ called a R_2 invariant representation. I shall start with a self-homotopy equivalence f of $(BO(2n)_2)^\wedge$ and find the possible admissible maps and R_2 invariant representations and then see which of these realise on $(BO(2n)_2)^\wedge$ as self-homotopy equivalences. The conclusion being, for each 2-adic unit k there are exactly two distinct self-homotopy equivalences of $(BO(2n)_2)^\wedge$ which act on T_γ in the manner $x \rightarrow x^k$ and this is a complete description.